

# 4.1 Breadth-First Search

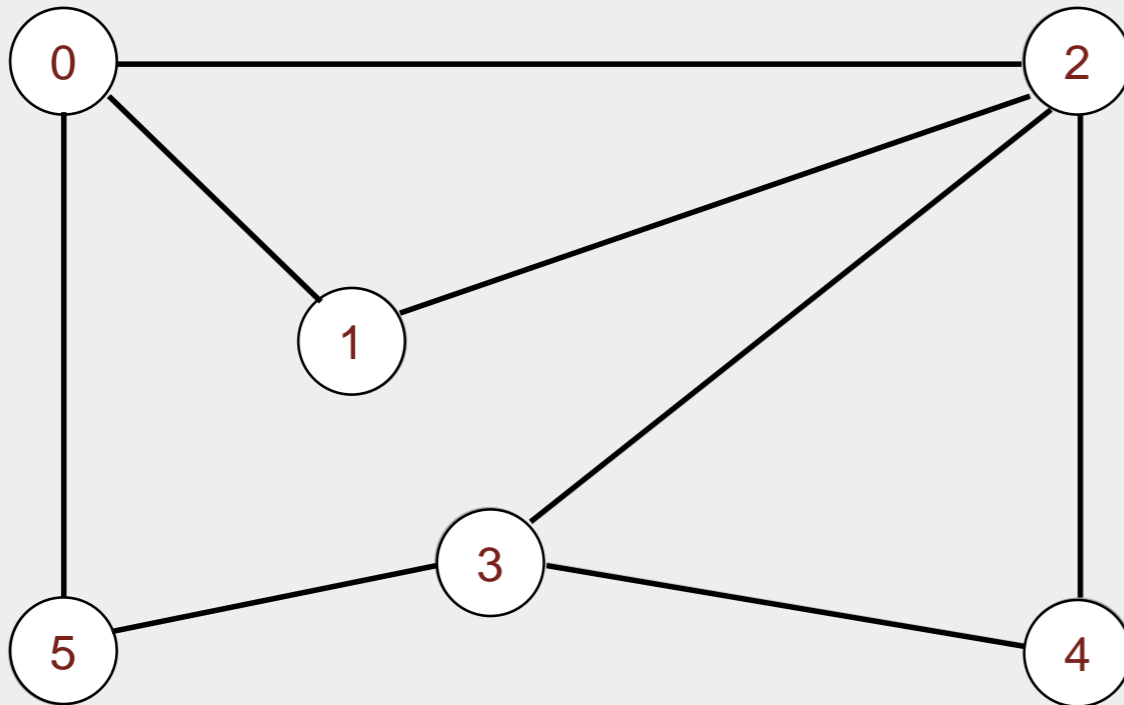


[click to begin demo](#)

# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.

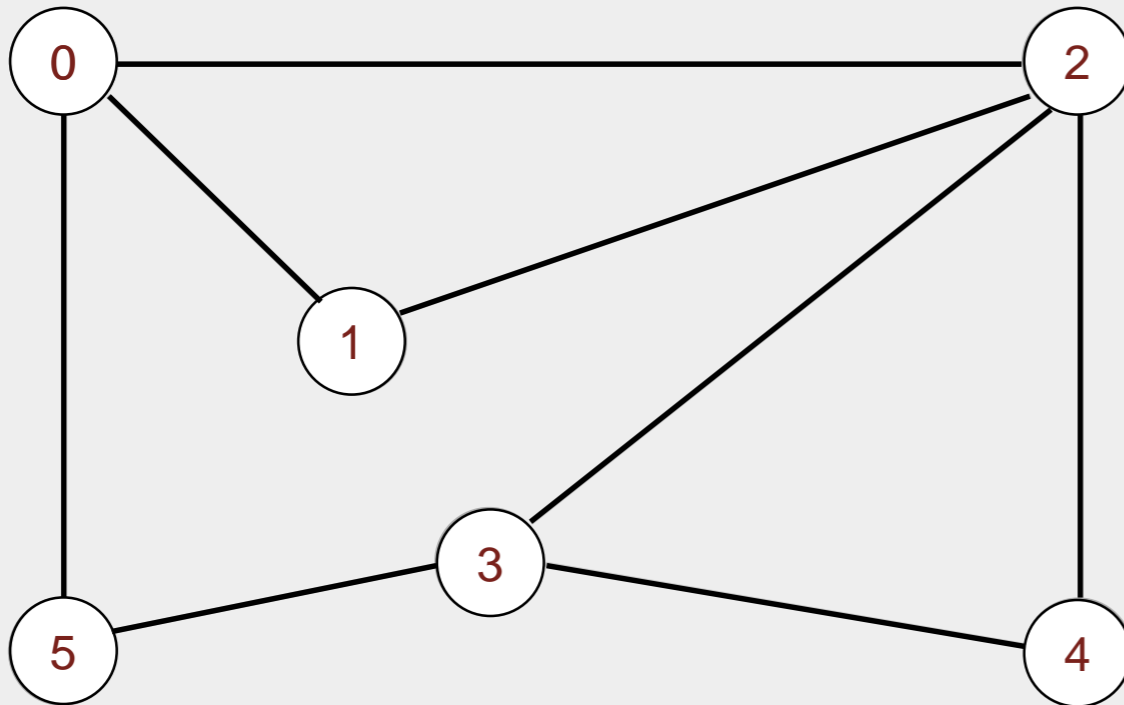


graph G

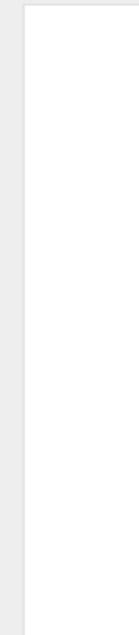
# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v edgeTo[v]

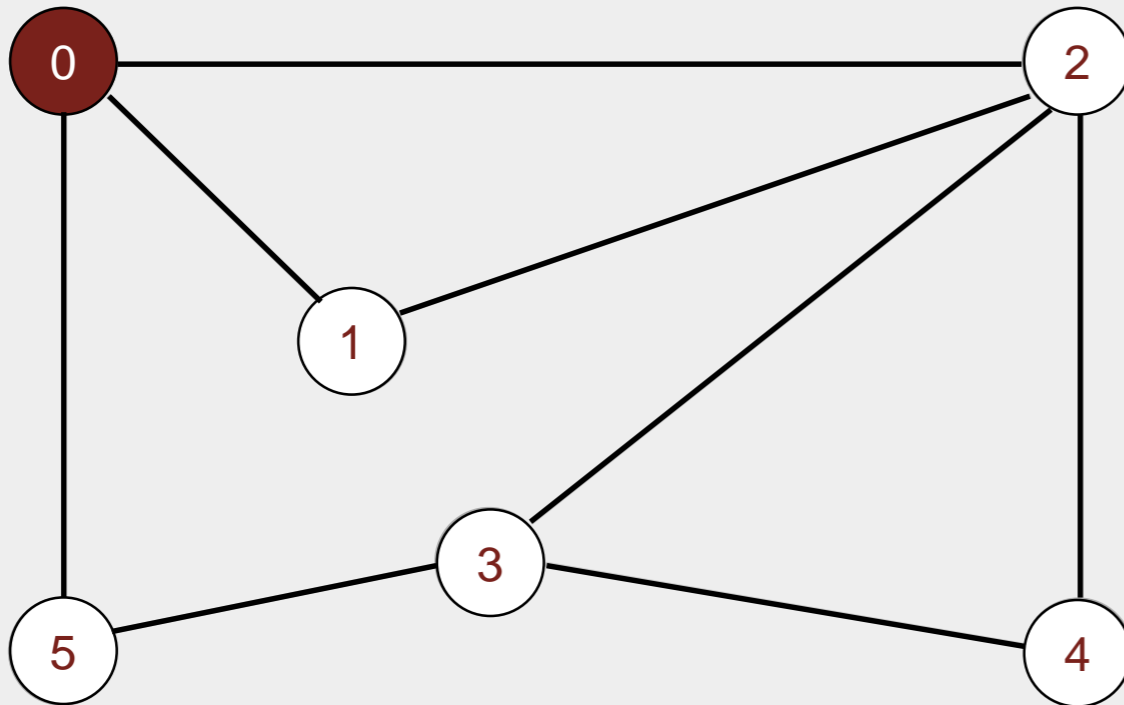
0	—
1	—
2	—
3	—
4	—
5	—

add 0 to queue

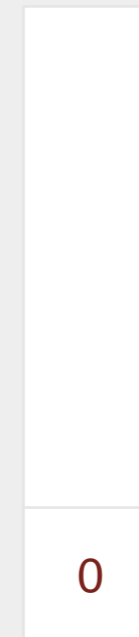
# Breadth-first search

Repeat until queue is empty:

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queue



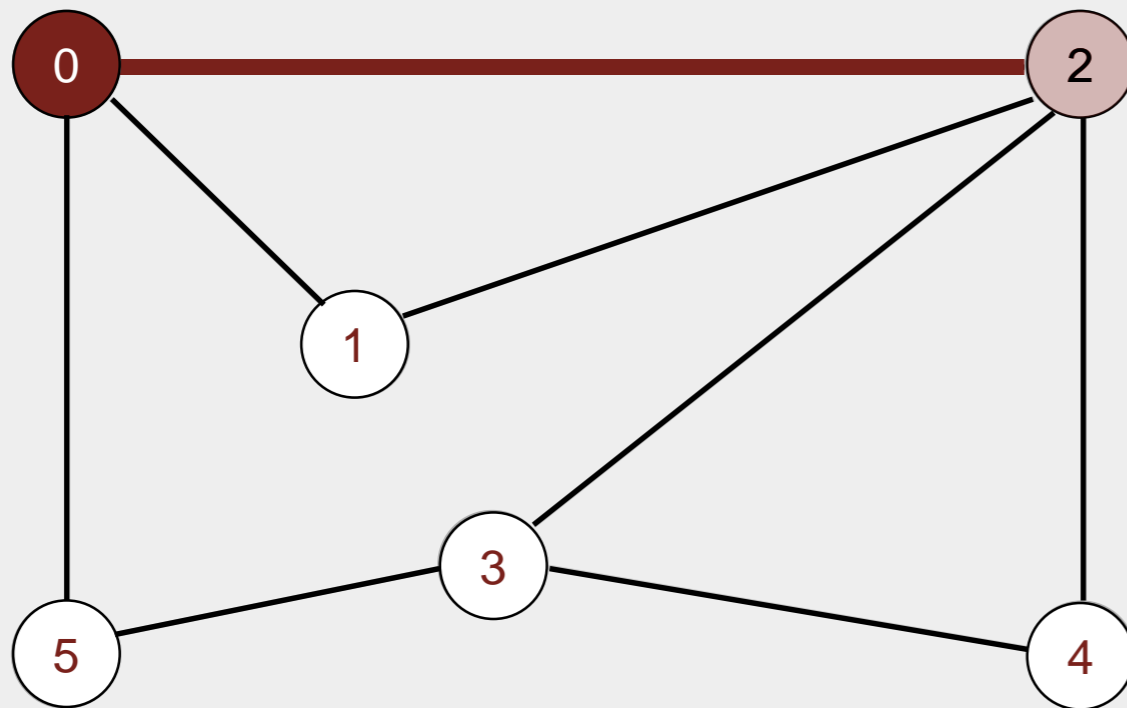
<u>v</u>	<u>edgeTo[v]</u>
0	—
1	—
2	—
3	—
4	—
5	—

**dequeue 0**

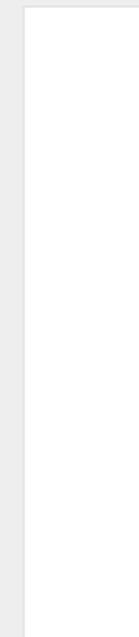
# Breadth-first search

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queue



v edgeTo[v]

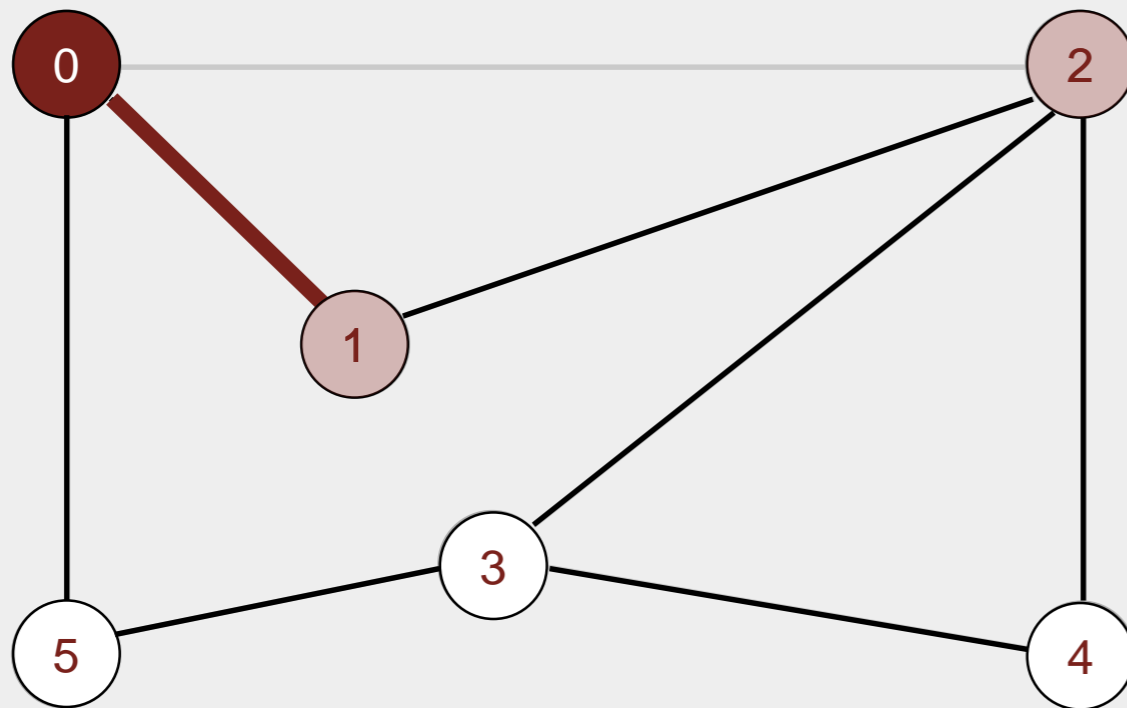
0	—
1	— 0
2	—
3	—
4	—
5	—

**dequeue 0**

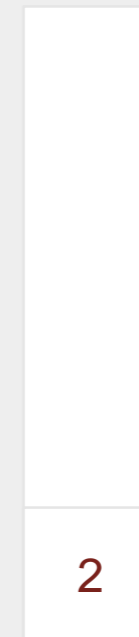
# Breadth-first search

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queue



v edgeTo[v]

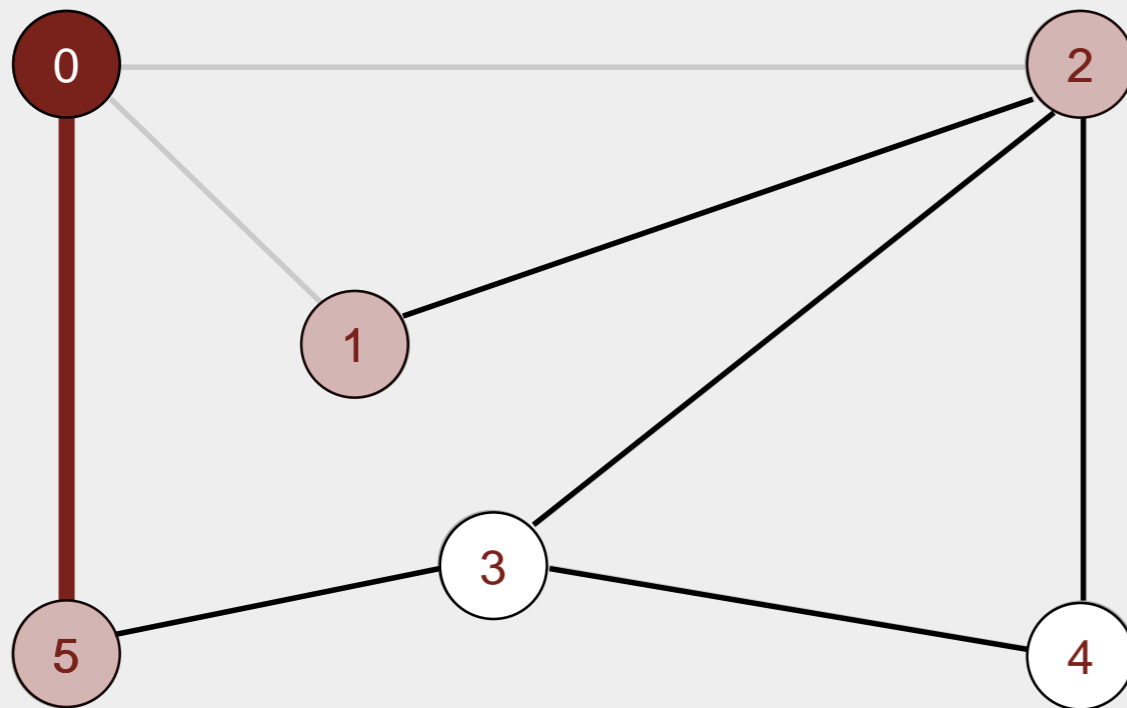
0	—
1	0
2	0
3	—
4	—
5	—

**dequeue 0**

# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v edgeTo[v]

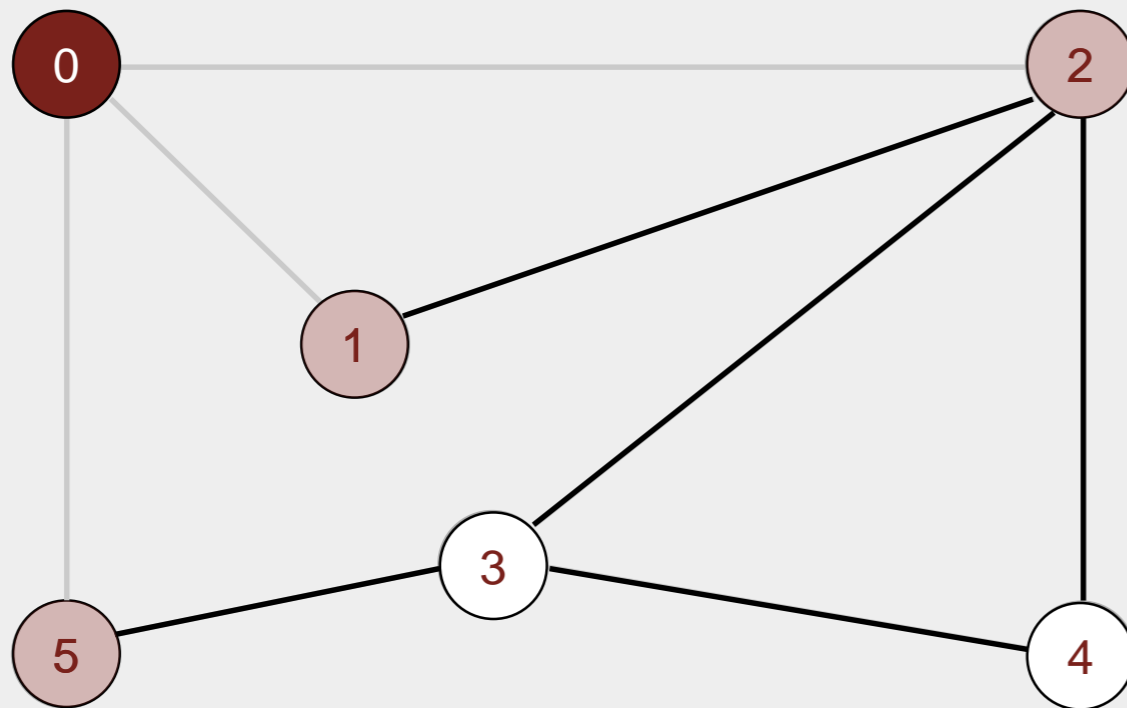
0	—
1	0
2	0
3	—
4	0
5	—

**dequeue 0**

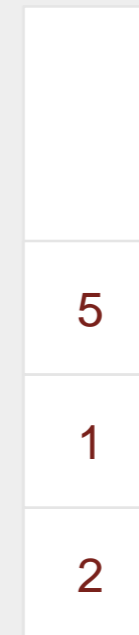
# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v edgeTo[v]

0	—
1	0
2	0
3	—
4	—
5	0

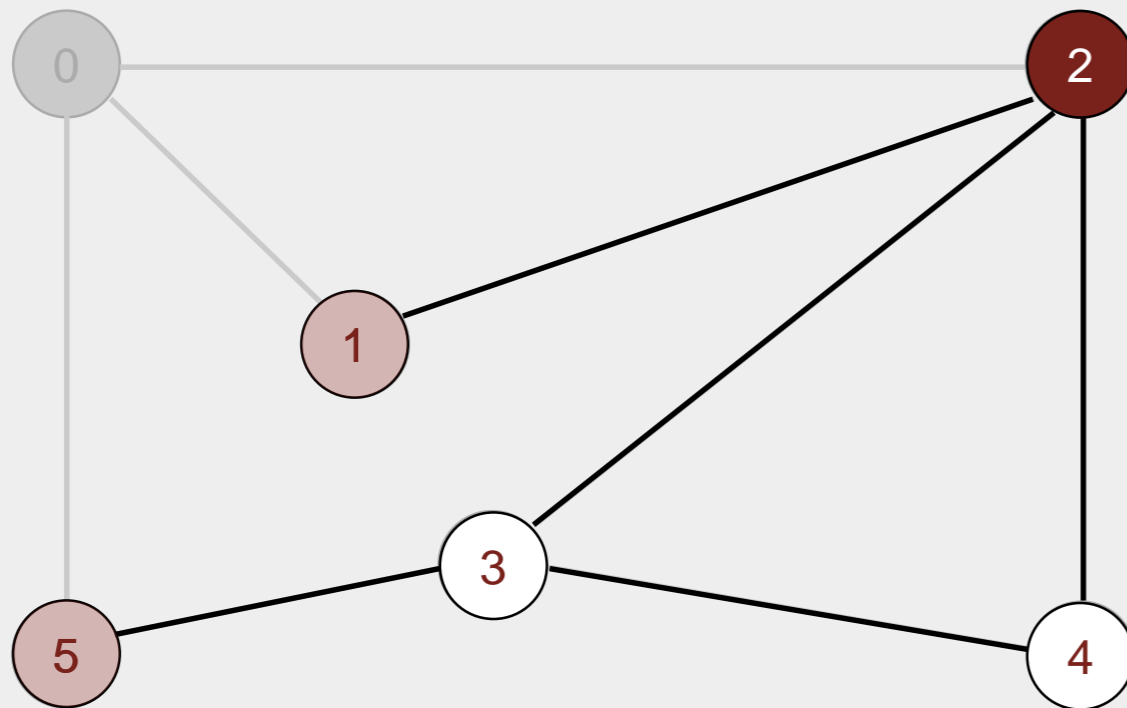
0 done



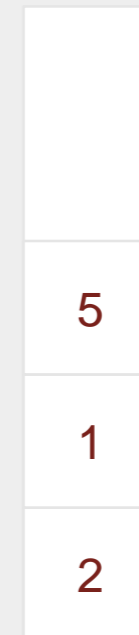
# Breadth-first search

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queue



v edgeTo[v]

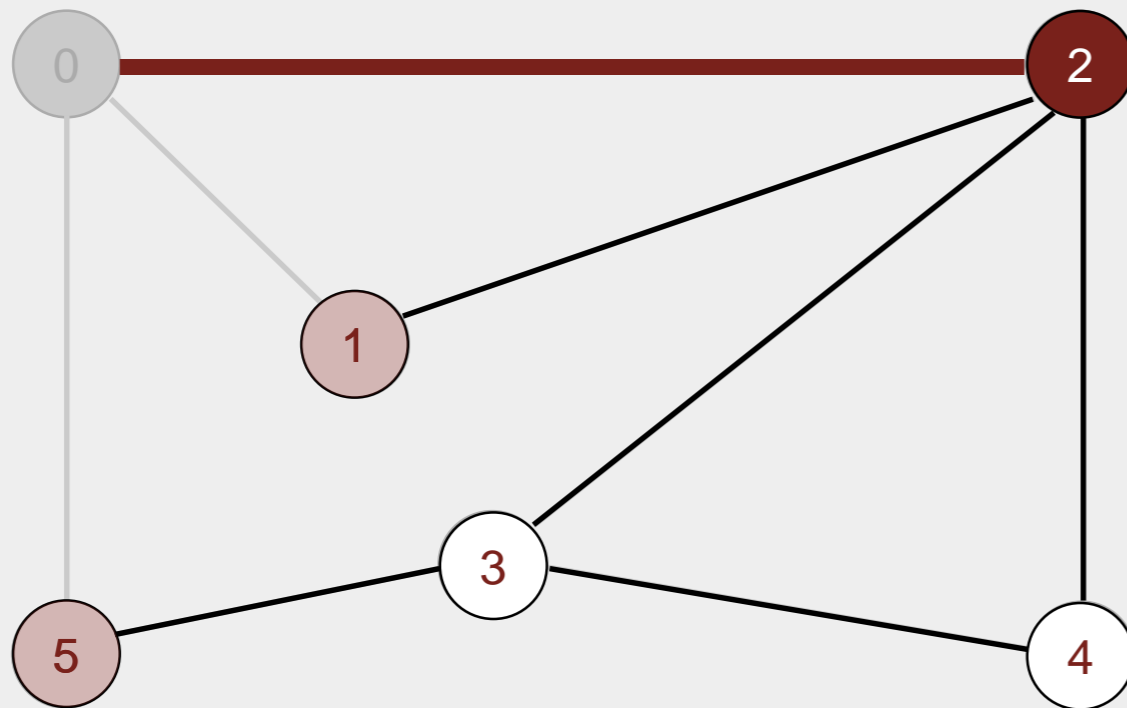
0	—
1	0
2	0
3	—
4	—
5	0

**dequeue 2**

# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v edgeTo[v]

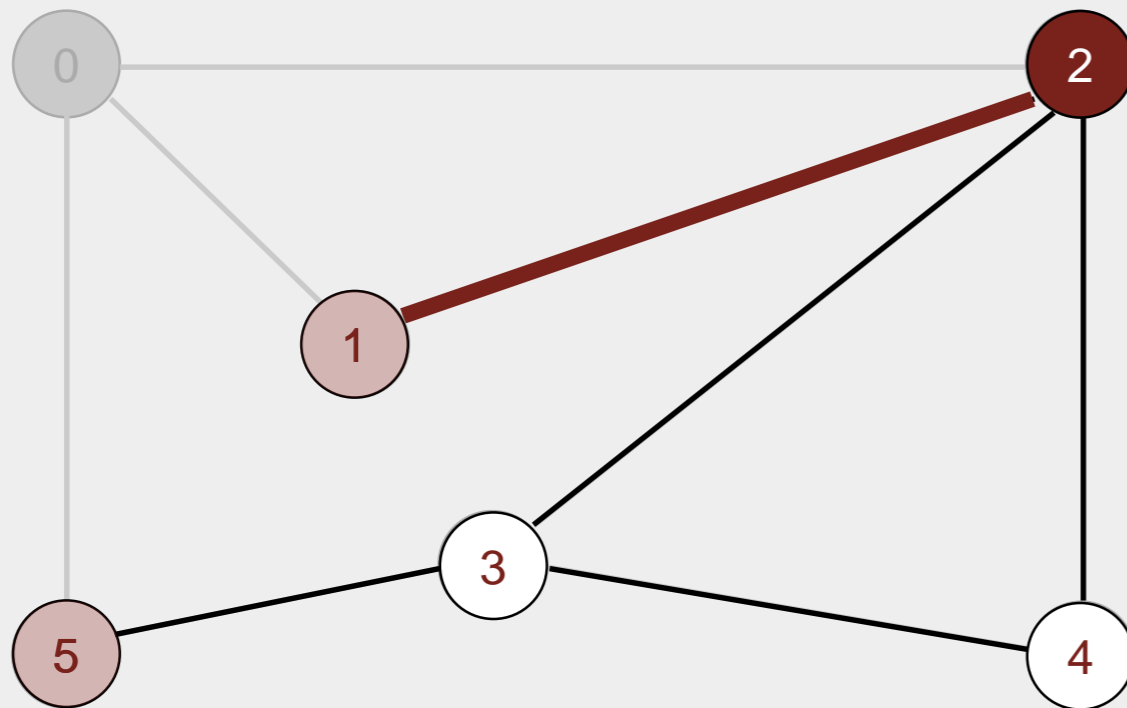
0	—
1	0
2	0
3	—
4	—
5	0

**dequeue 2**

# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v edgeTo[v]

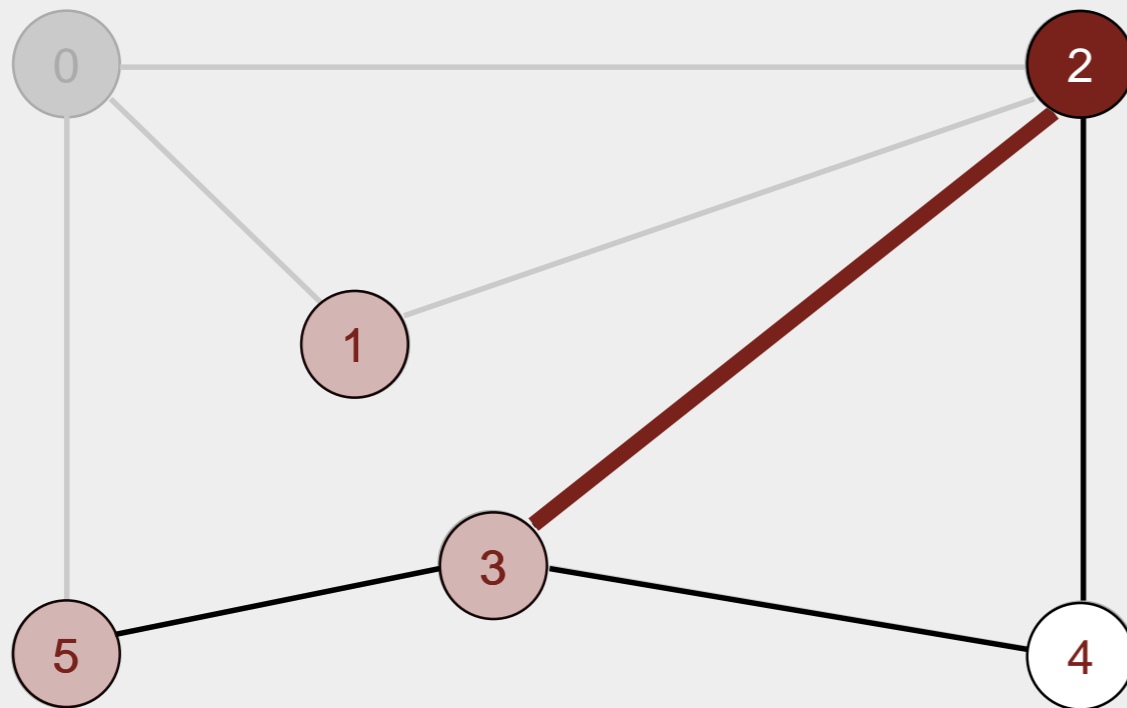
0	—
1	0
2	0
3	—
4	—
5	0

**dequeue 2**

# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v edgeTo[v]

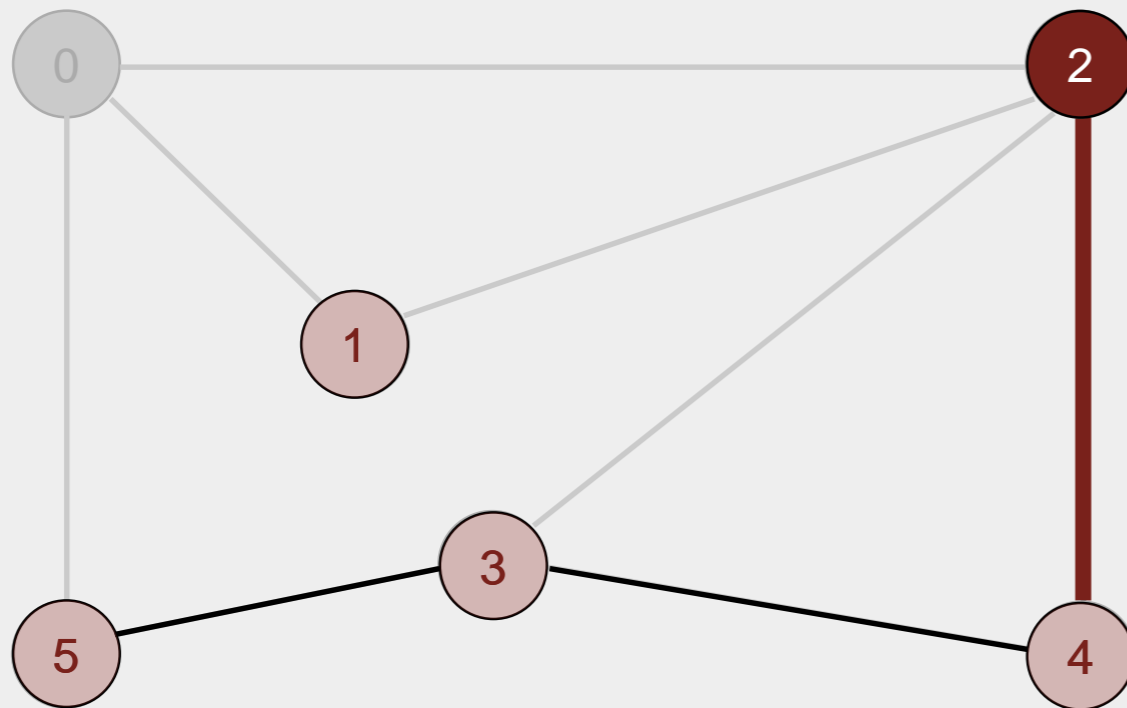
0	-
1	0
2	2
3	-
4	-
5	0

**dequeue 2**

# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v    edgeTo[v]

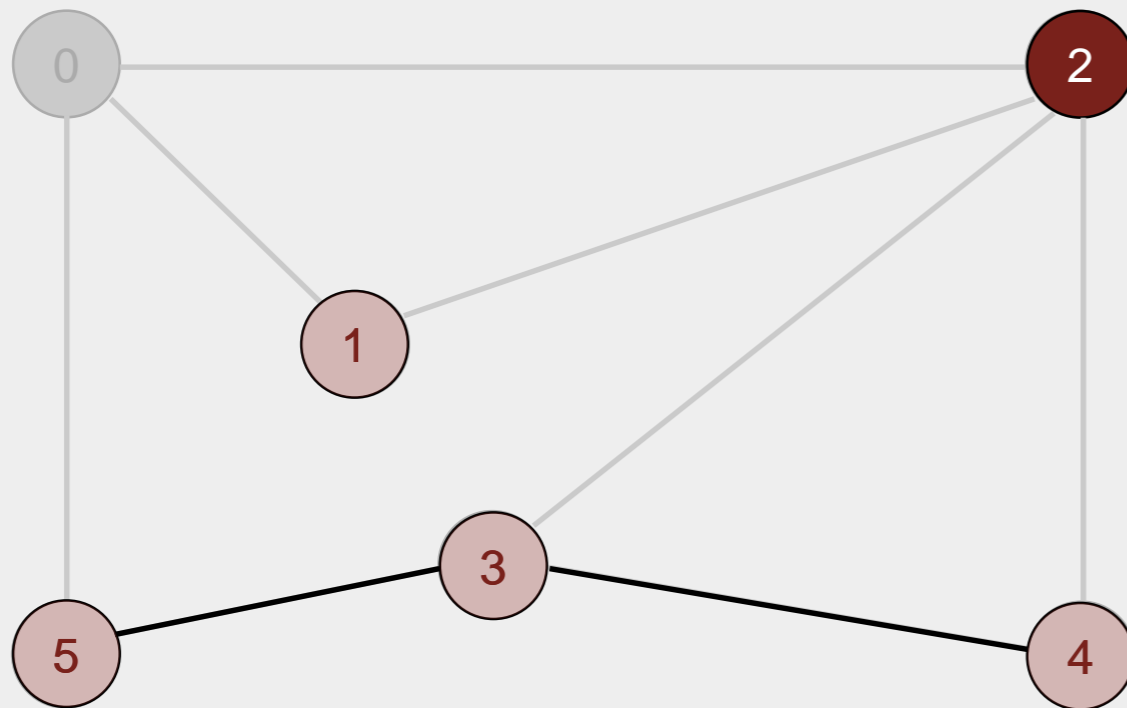
0	—
1	0
2	0
3	2
4	—
5	0

**dequeue 2**

# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue

4
3
5
1

v edgeTo[v]

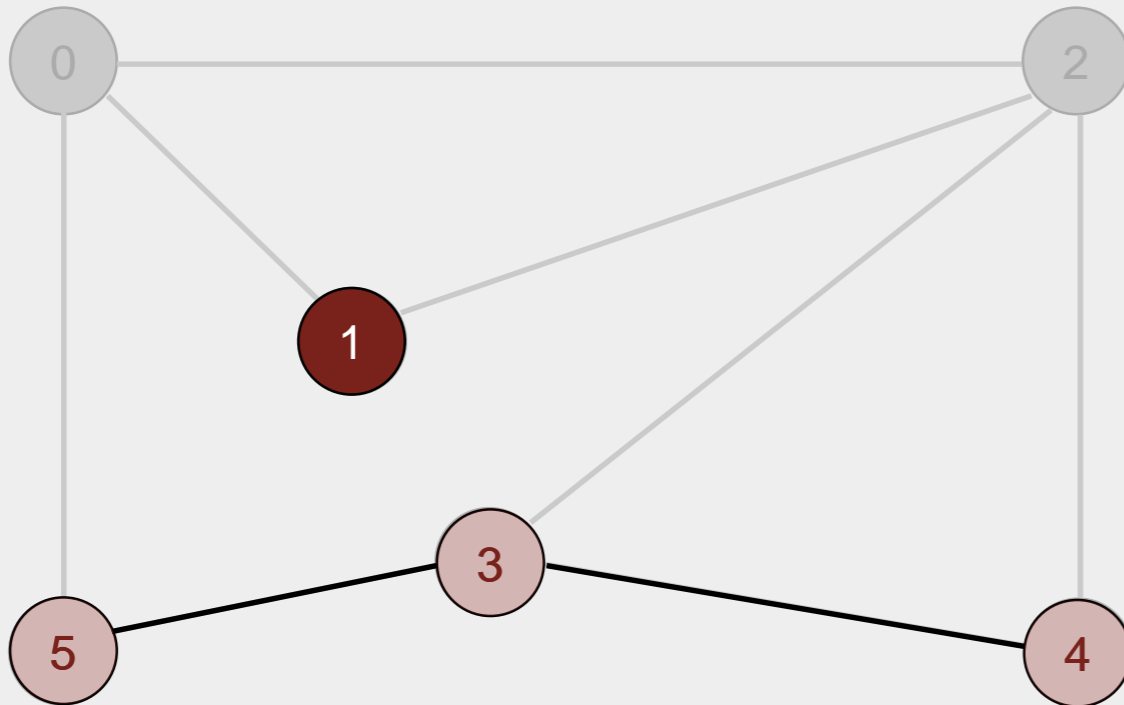
0	-
1	0
2	0
3	2
4	2
5	0

**2 done**

# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue

4
3
5
1

v   edgeTo[v]

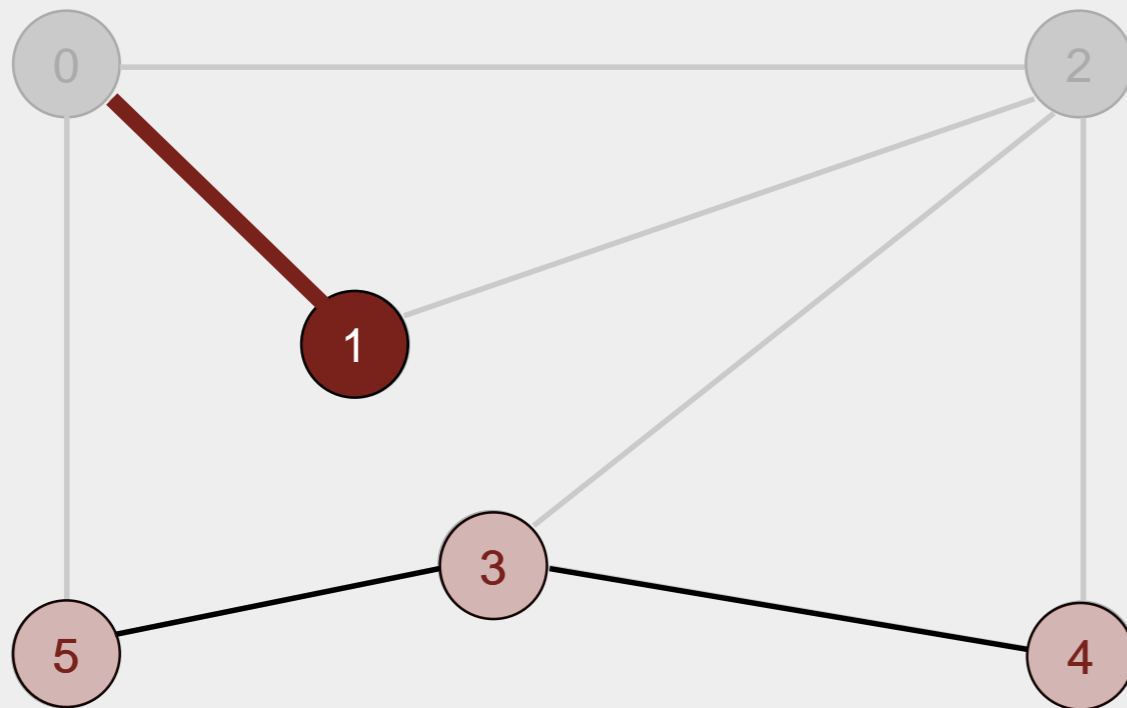
0	—
1	0
2	0
3	2
4	2
5	0

dequeue 1

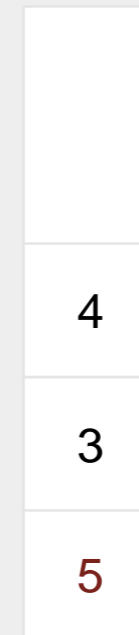
# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v edgeTo[v]

0	—
1	0
2	0
3	2
4	2
5	0

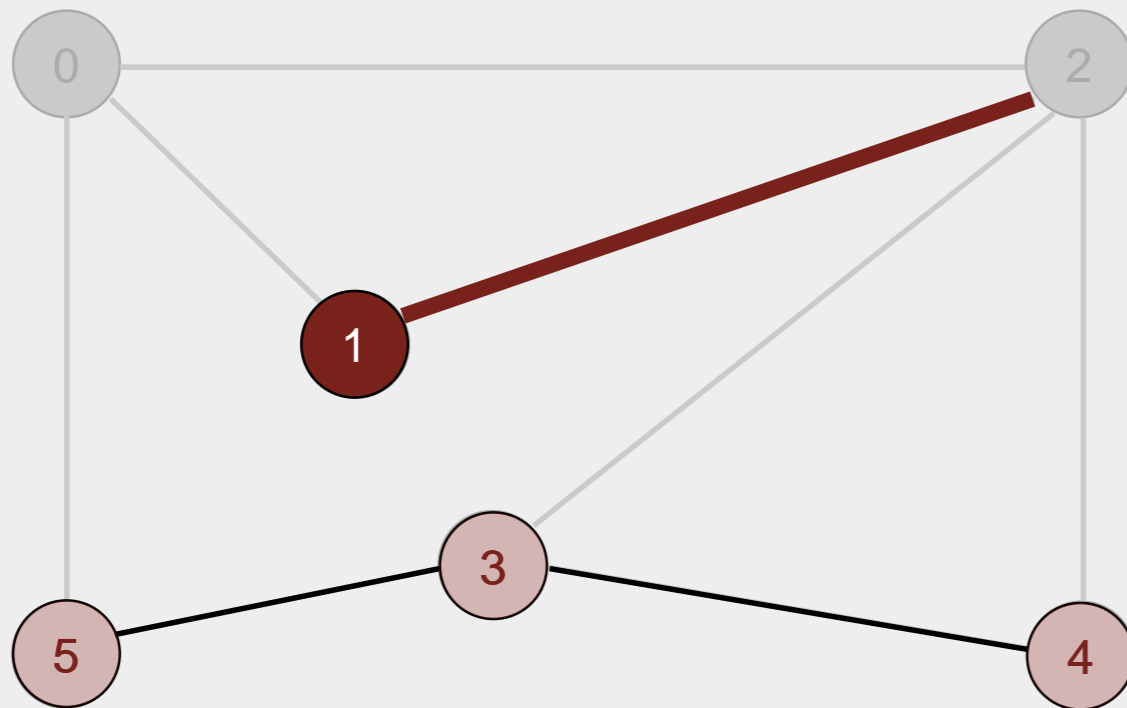
**dequeue 1**



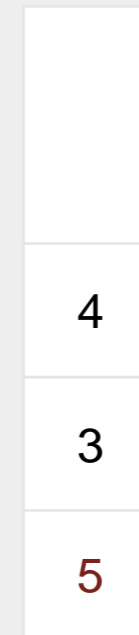
# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v    edgeTo[v]

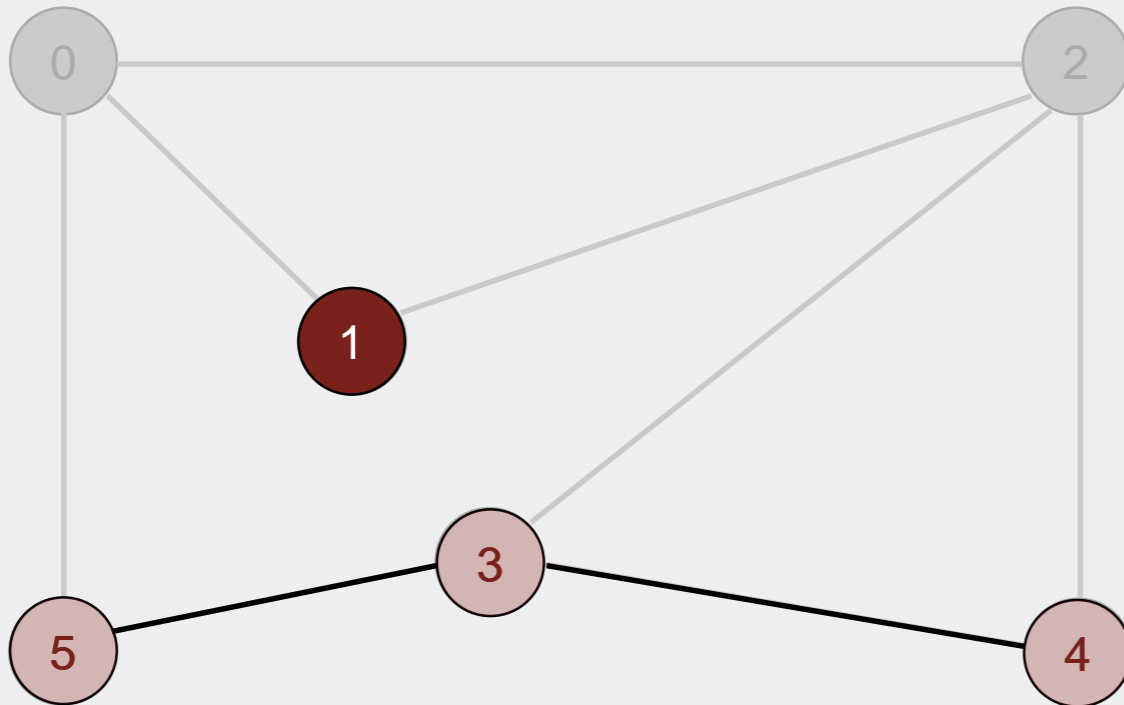
0	—
1	0
2	0
3	2
4	2
5	0

dequeue 1

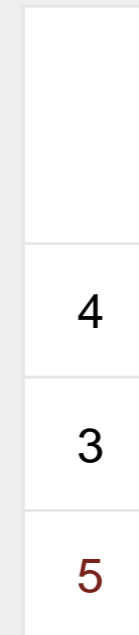
# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v   edgeTo[v]

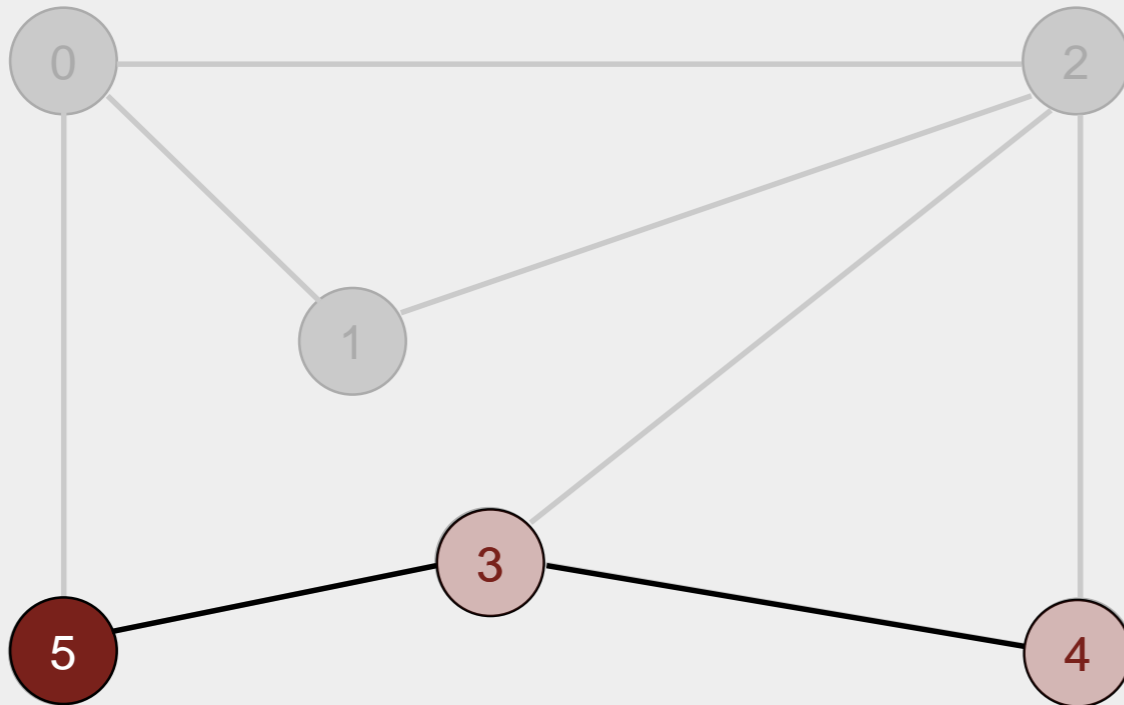
0	—
1	0
2	0
3	2
4	2
5	0

**1 done**

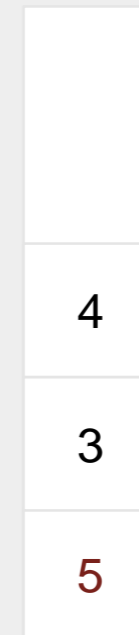
# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v   edgeTo[v]

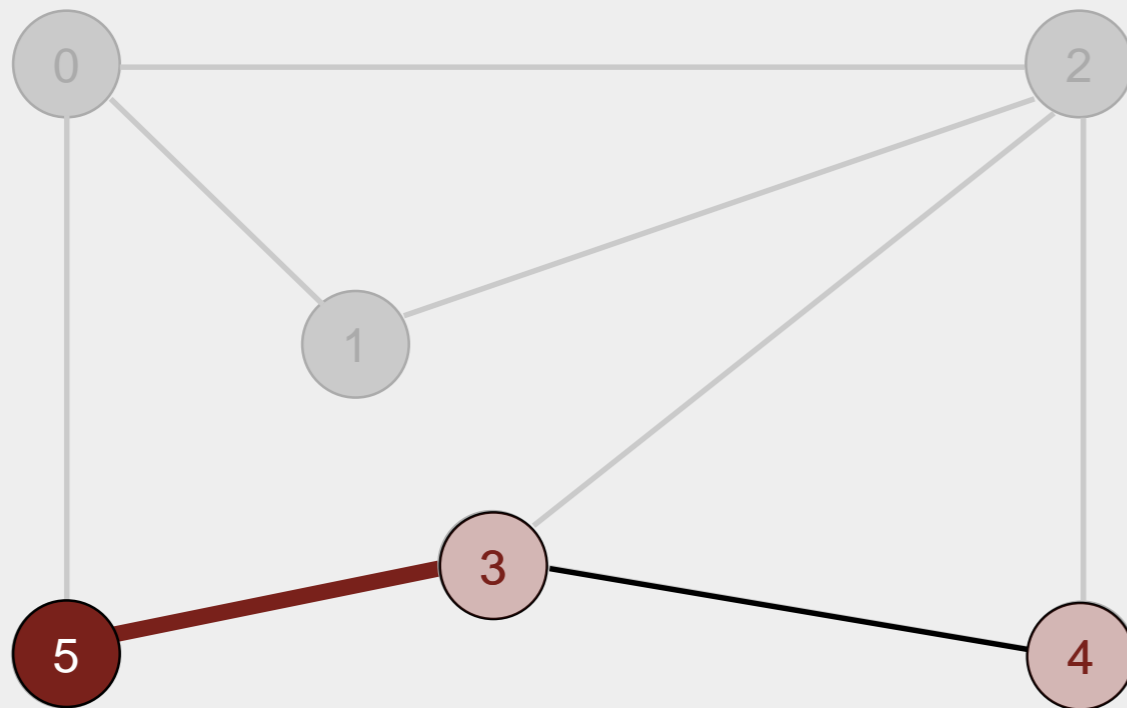
0	—
1	0
2	0
3	2
4	2
5	0

**dequeue 5**

# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v edgeTo[v]

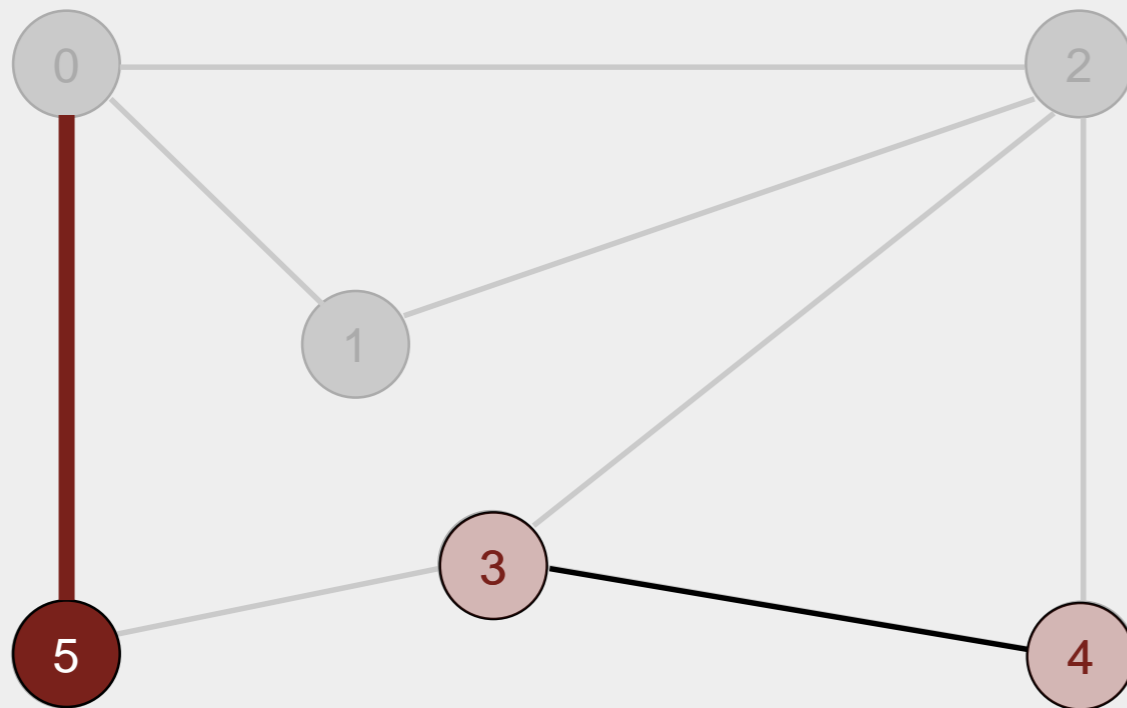
0	—
1	0
2	0
3	2
4	2
5	0

**dequeue 5**

# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v edgeTo[v]

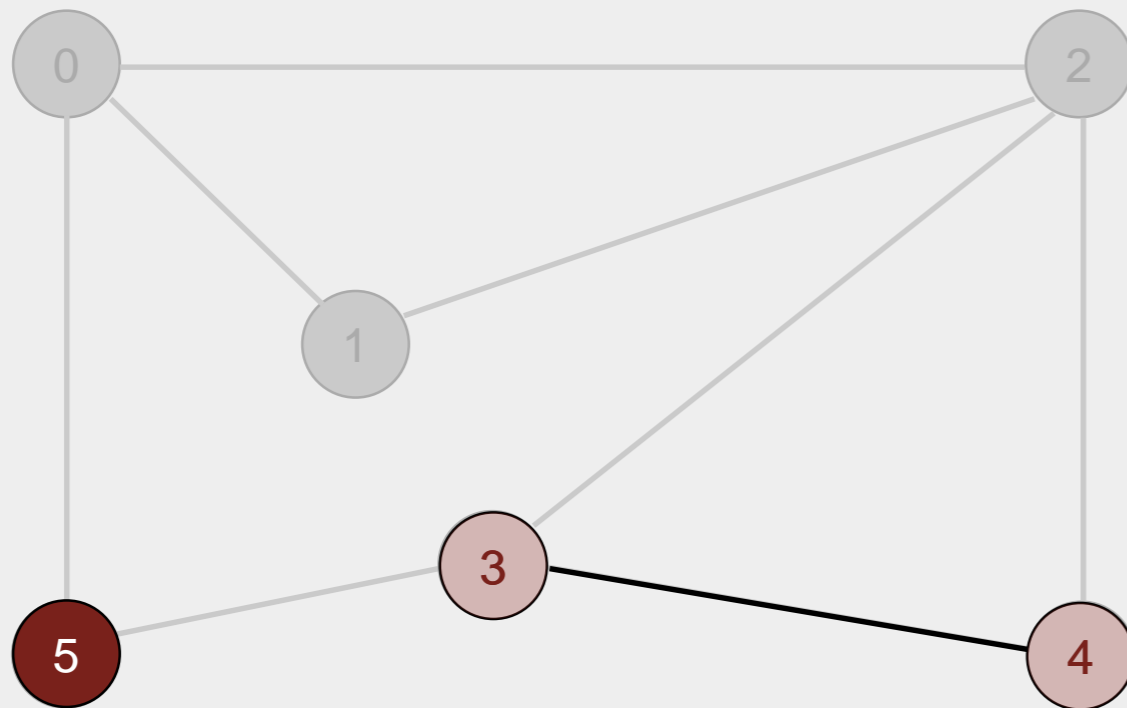
0	—
1	0
2	0
3	2
4	2
5	0

**dequeue 5**

# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v    edgeTo[v]

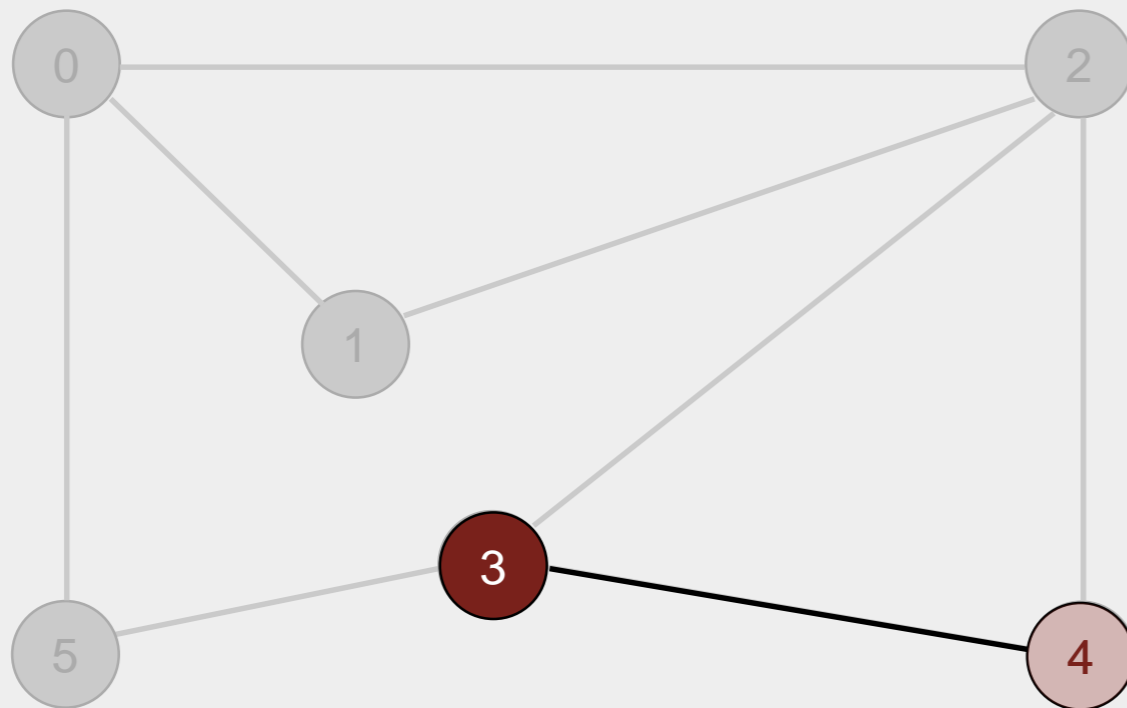
0	—
1	0
2	0
3	2
4	2
5	0

5 done

# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v edgeTo[v]

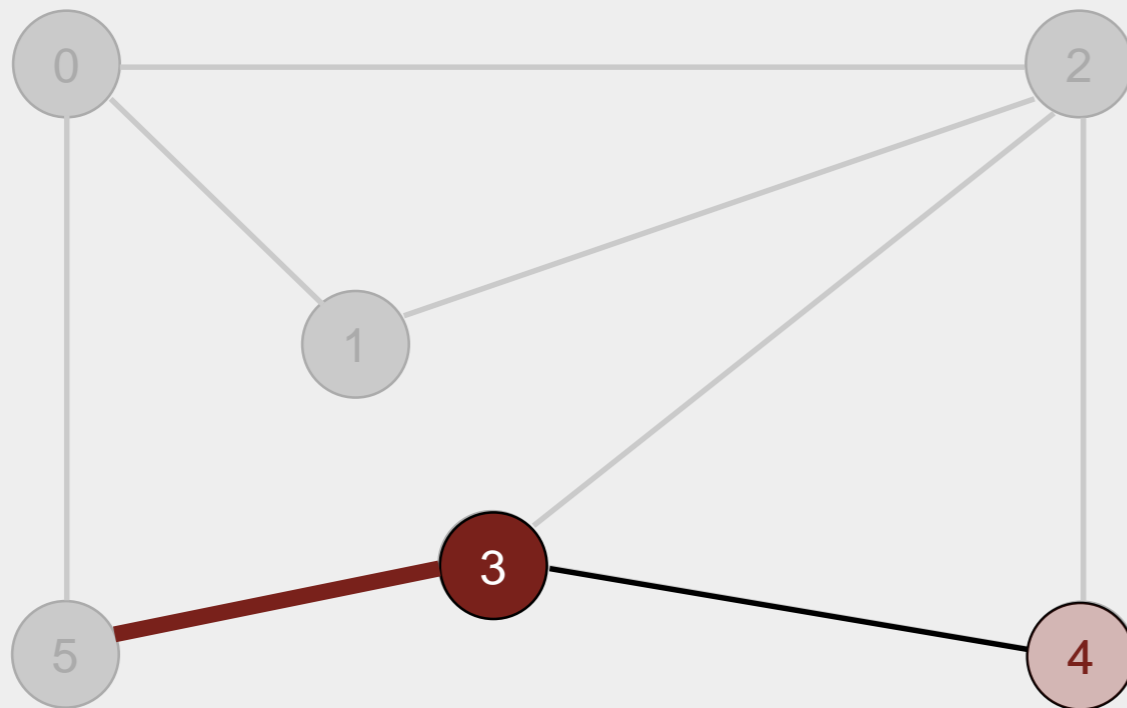
0	-
1	0
2	0
3	2
4	2
5	0

**dequeue 3**

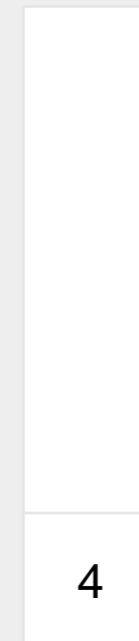
# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



<u>v</u>	<u>edgeTo[v]</u>
0	—
1	0
2	0
3	2
4	2
5	0

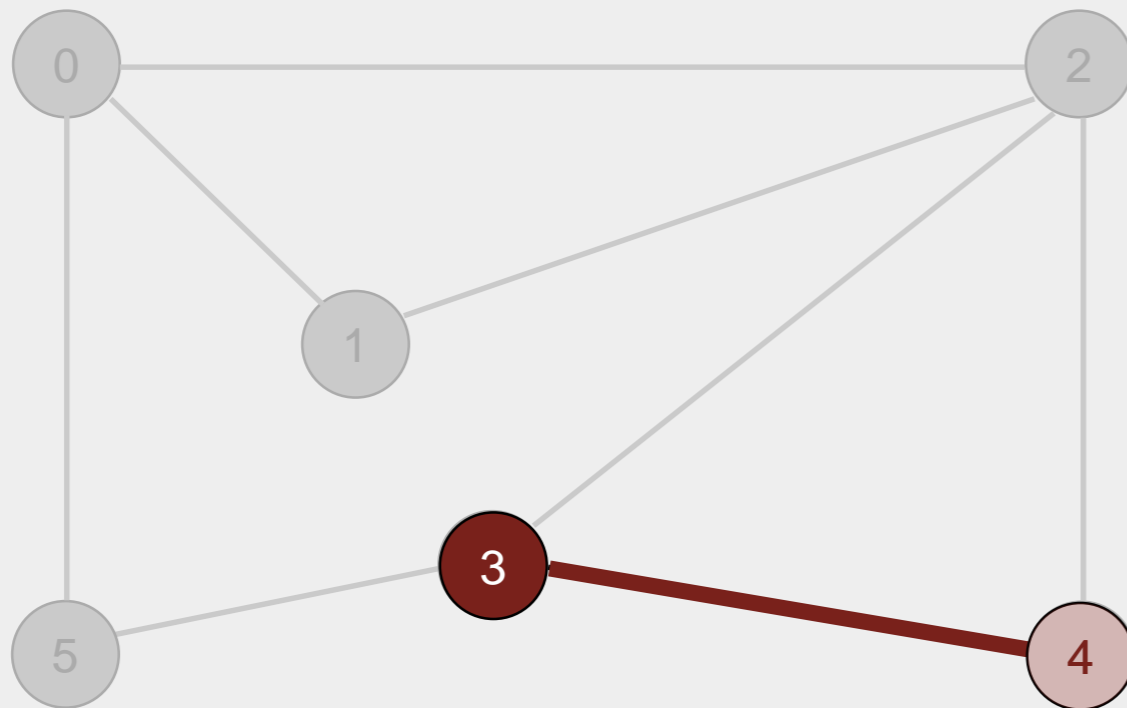
**dequeue 3**



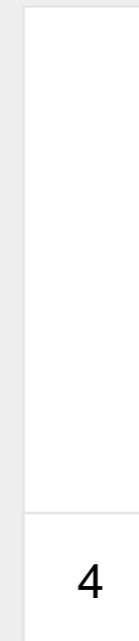
# Breadth-first search

Repeat until queue is empty:

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- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v   edgeTo[v]

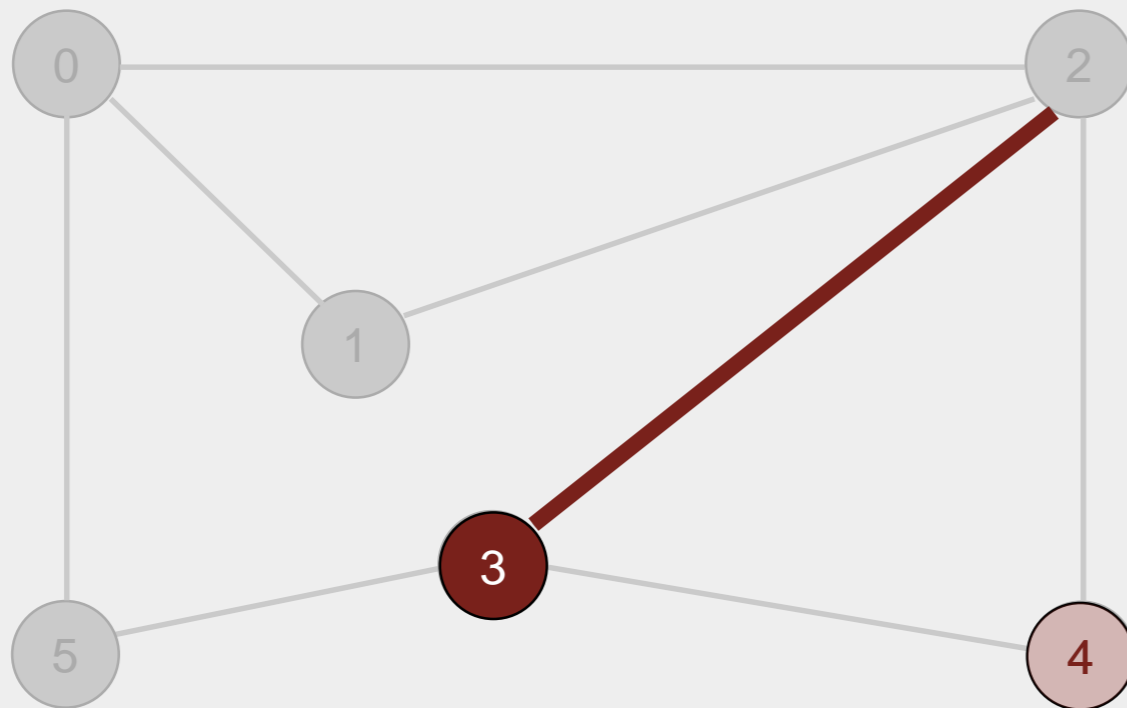
0	—
1	0
2	0
3	2
4	2
5	0

**dequeue 3**

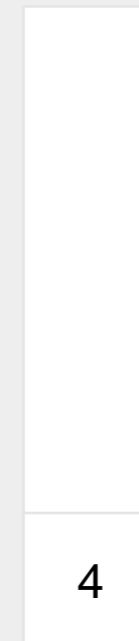
# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



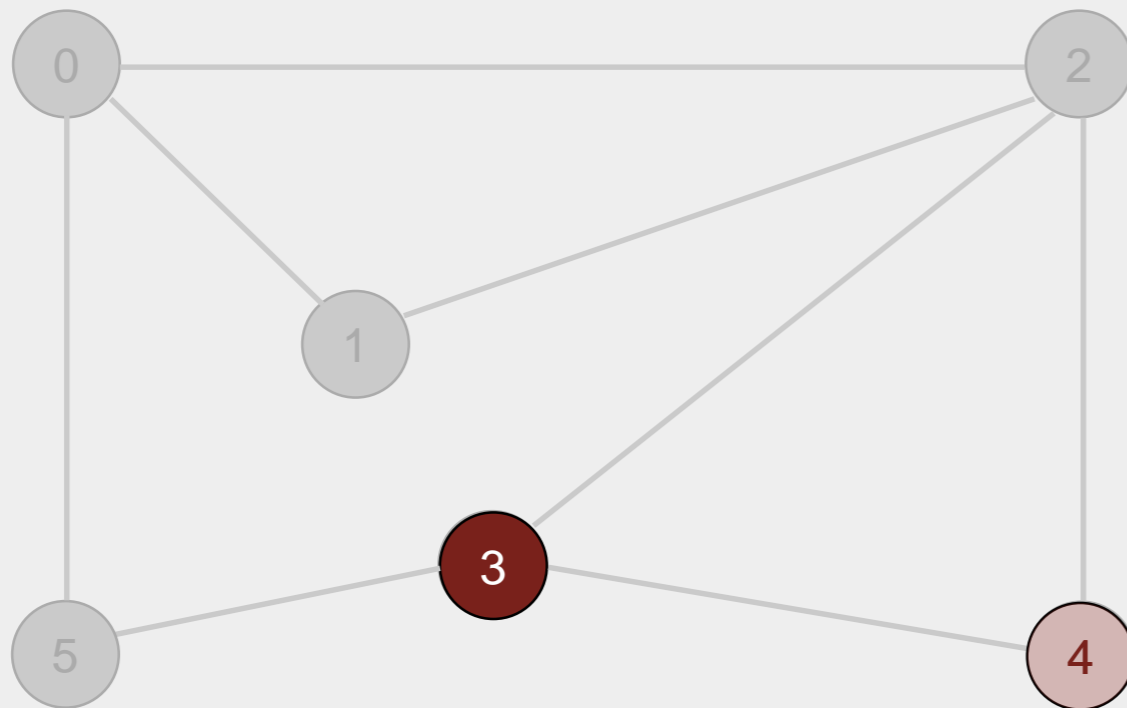
<u>v</u>	<u>edgeTo[v]</u>
0	—
1	0
2	0
3	2
4	2
5	0

**dequeue 3**

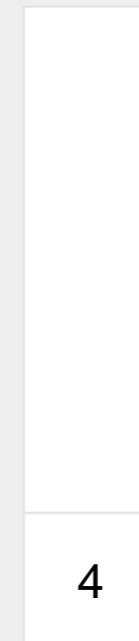
# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v    edgeTo[v]

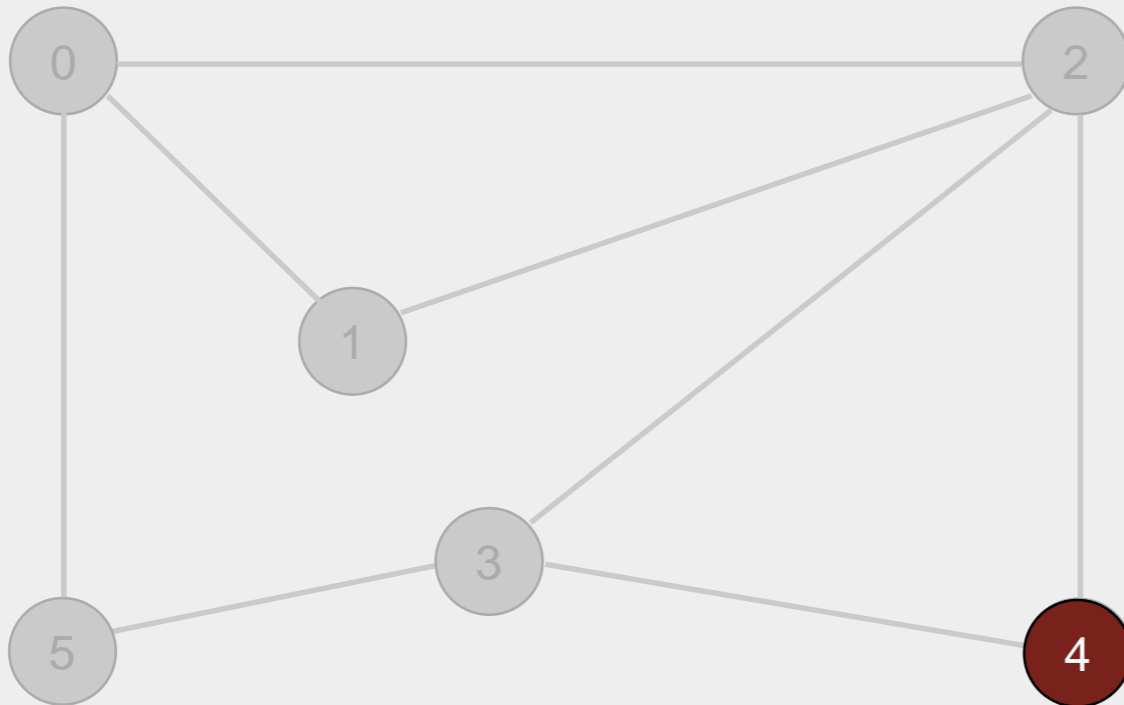
0	—
1	0
2	0
3	2
4	2
5	0

**3 done**

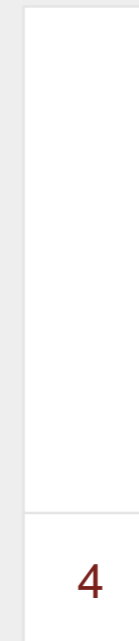
# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



v    edgeTo[v]

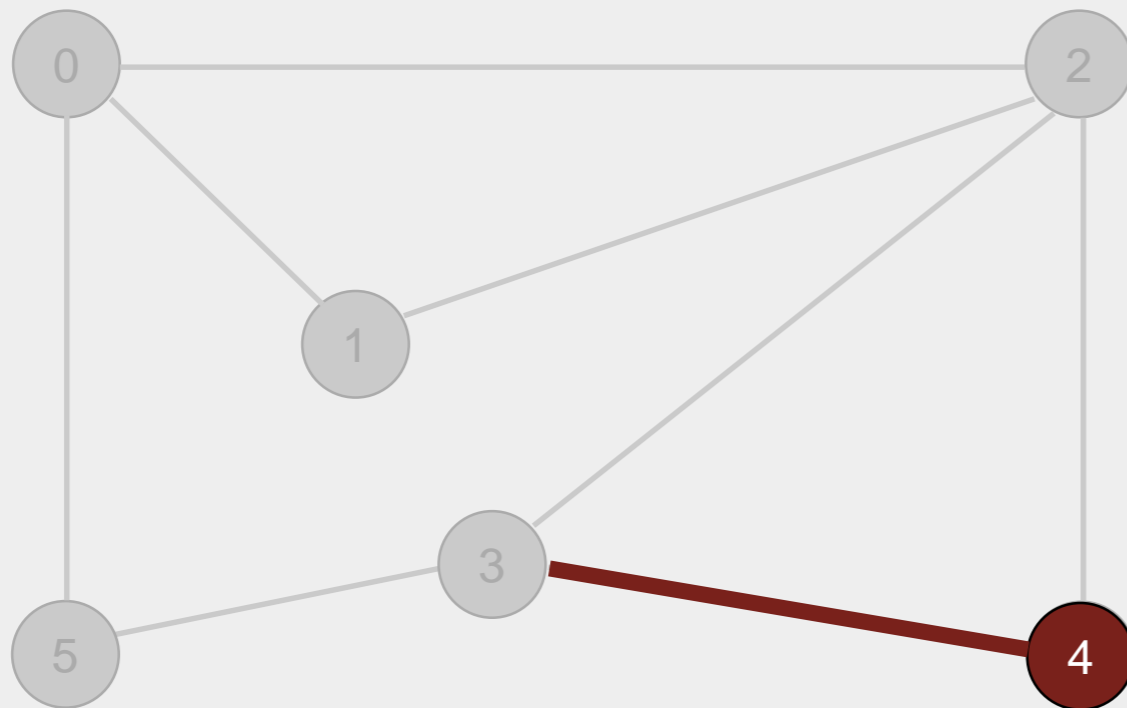
0	—
1	0
2	0
3	2
4	2
5	0

**dequeue 4**

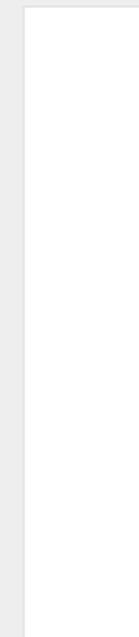
# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



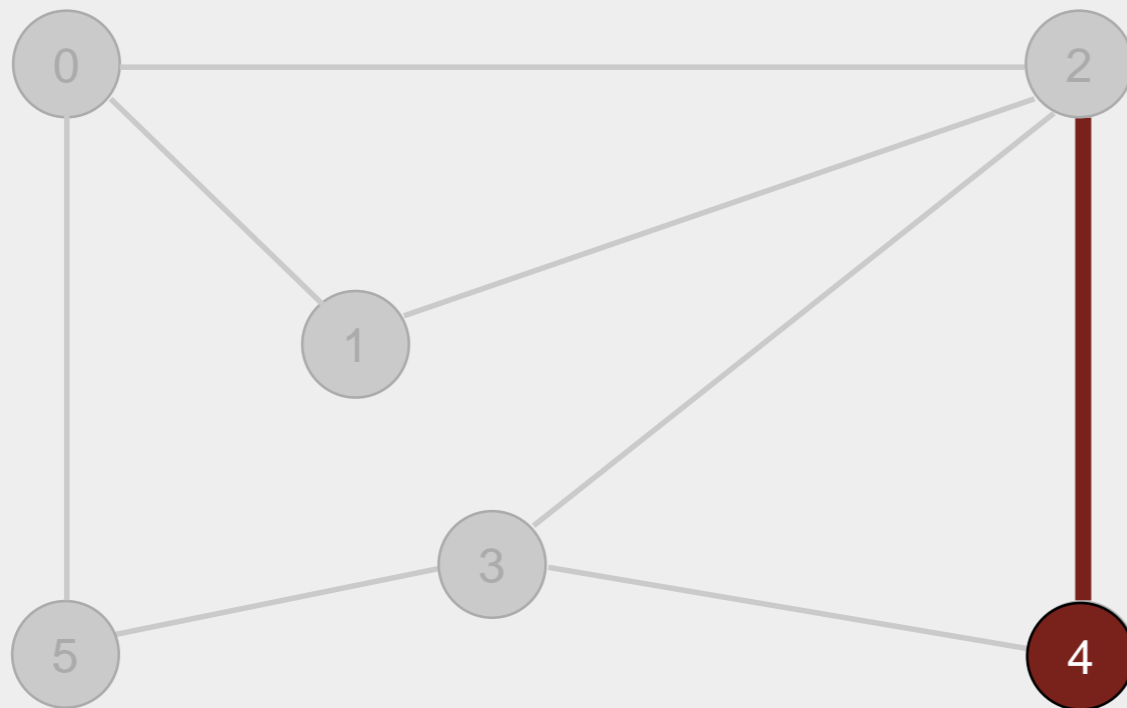
<u>v</u>	<u>edgeTo[v]</u>
0	—
1	0
2	0
3	2
4	2
5	0

**dequeue 4**

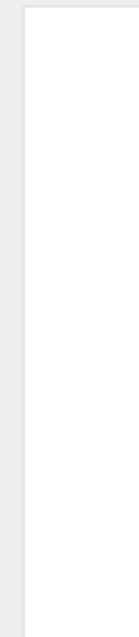
# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



queue



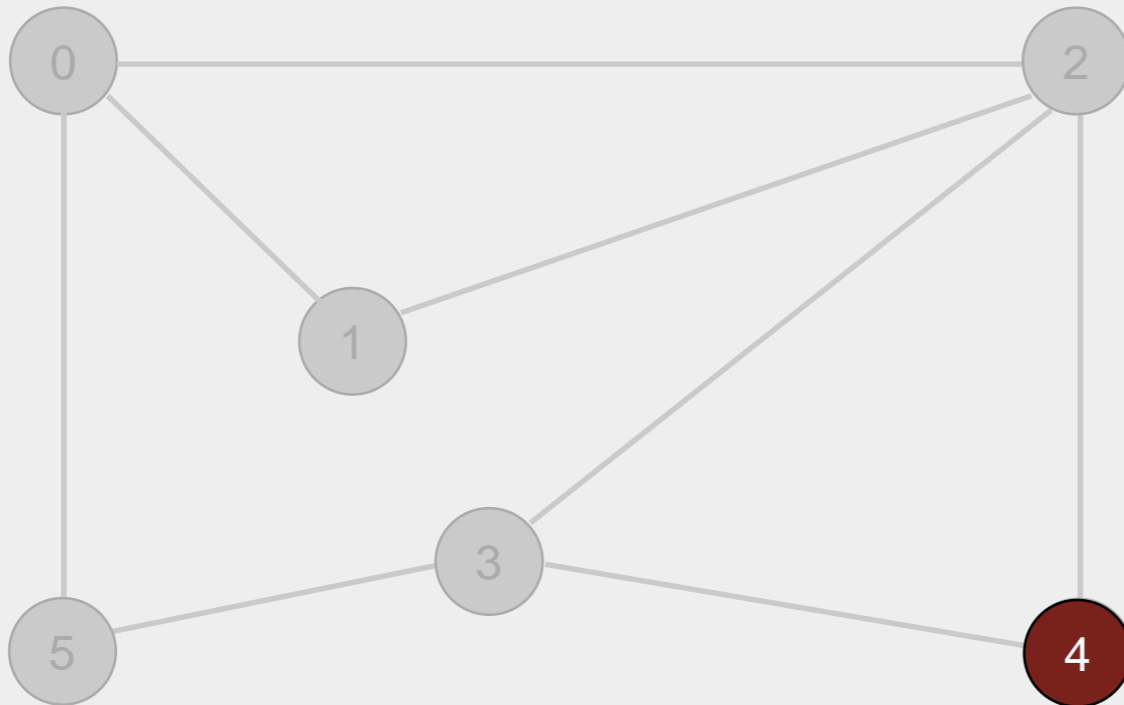
<u>v</u>	<u>edgeTo[v]</u>
0	—
1	0
2	0
3	2
4	2
5	0

**dequeue 4**

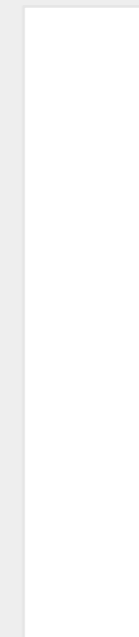
# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
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queue



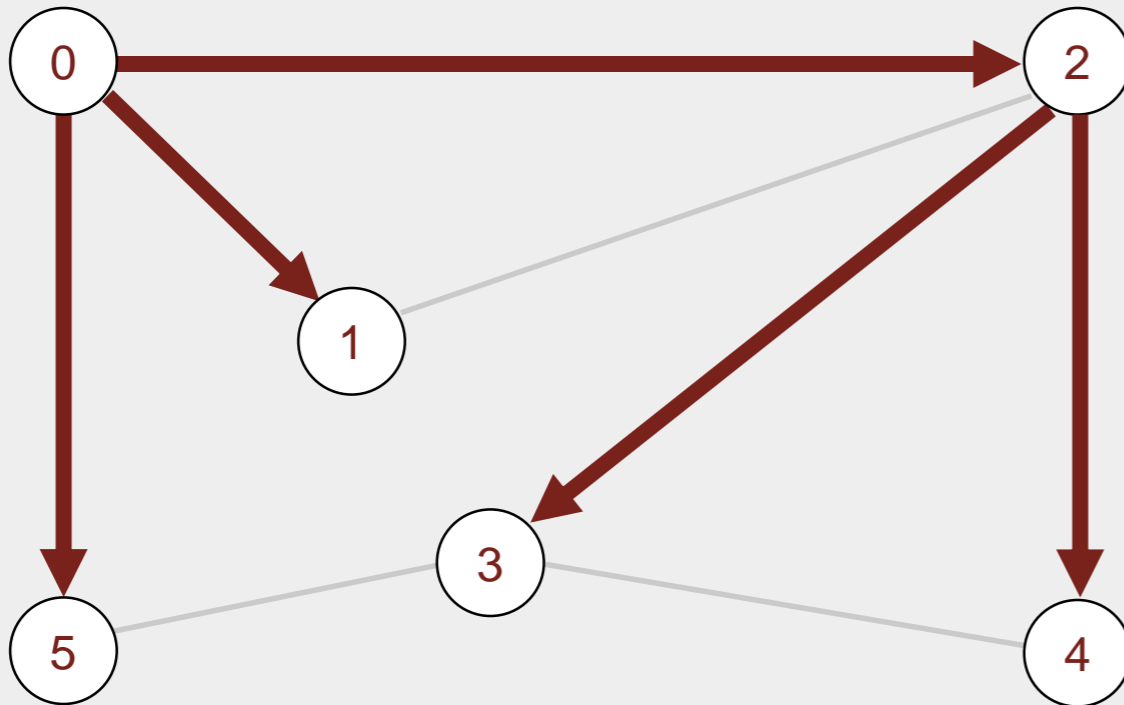
<u>v</u>	<u>edgeTo[v]</u>
0	—
1	0
2	0
3	2
4	2
5	0

**4 done**

# Breadth-first search

Repeat until queue is empty:

- Remove vertex  $v$  from queue.
- Add to queue all unmarked vertices adjacent to  $v$  and mark them.



$v$	edgeTo[ $v$ ]
0	—
1	0
2	0
3	2
4	2
5	0

done